#### Off-Axis-NOTE-SIM-12

## A Study of an Off-axis Detector Performance as a Function of Sampling Frequency

L.Camilleri, A. Para

#### Abstract

This memo describes the studies made to determine the dependence of the sensitivity of an off-axis detector as a function of the sampling frequency (the thickness of the absorber placed between successive active planes). This involved optimizing the cuts used in the rejection of background from  $\nu_{\mu}$ NC,  $\nu_{\mu}$ CC and beam  $\nu_{e}$  while maintaining a high efficiency for the oscillation signal:  $\nu_{\mu} \rightarrow \nu_{e}$ .

## 1 The generated event sample

The generation of Monte Carlo events and their reconstruction was described in a previous memo [1]. The basic geometry, Fig. 1 used consisted in the following sequence of material:

- zair cm of air,
- zpla cm of plastic,
- a glass RPC with X and Y readout, amounting to 5% of a radiation length..

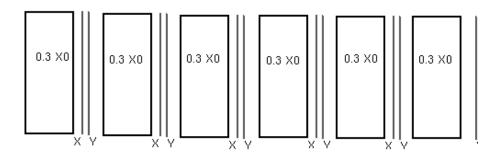


Figure 1: An example of the distribution of absorber and x,y readout planes

**zair** and **zpla** were chosen such as to yield a material with density equal to  $0.7~\rm gm.cm^{-3}$ , the density of particle board which will probably be used in the detector.

Event samples with two different geometries, described in Table 1, were generated for the analysis described in this note.

Table 1: Geometries generated for the analysis

$_{ m cair}$	zpla (cm)	RPC (% rad.len)	Total sampling frequency (% rad.len)
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5	12.5	5	30
-2.5	6.25	5	17.5

By ignoring the X **AND** Y read out of every other RPC in the 30% radiation length sample of events, a third sampling frequency, namely 60% of a radiation length, could also be studied.

Furthermore, by ignoring the Y read out in the odd planes and the X readout in the even planes, a detector with alternate X **OR** Y readout in successive planes could also be studied.

The read out strip width was taken to be 3cm.

For each of the geometries studied charged current (CC) and neutral current (NC) interactions for both  $\nu_{\mu}$  and  $\nu_{e}$  were generated. The  $\nu_{\mu}$  interactions were used to study the background. The  $\nu_{e}$  interactions were used to study both the intrinsic  $\nu_{e}$  background present in the beam and the signal from  $\nu_{\mu} \rightarrow \nu_{e}$  oscillations.

For the 30% radiation length sampling frequency geometry  $\bar{\nu}_{\mu}$  and  $\bar{\nu}_{e}$  samples of events were also generated.

### 2 Ntuple generation

For each of the two geometries, the events were reconstructed and Ntuples were generated using the program described in [1]. These samples are referred to as 6CM and 12CM.

By ignoring the read out of every other RPC in the 30% radiation length sample of events, a third sampling frequency, namely 60% of a radiation length, could also be studied. This is referred to as DOUBLE.

Furthermore, by ignoring the Y read out in the odd planes and the X readout in the even planes, a detector with alternate X or Y readout in successive planes could also be studied. This is referred to as XORY.

The antineutrino run with 30% radiation length sampling is referred to as 12BAR.

These ntuples are stored in the directory:

/afs/fnal.gov/files/code/off-axis/off-axis\_02/ntuples.

The ntuples for the five configurations, 6CM, 12CM, DOUBLE, XORY and 12BAR are stored in separate subdirectories as listed in Table 2.

Table 2: Storage and number of files available (10000 events per file)

Configuration	Subdirectory for $\nu_e,  \bar{\nu}_e$	Subdirectory for $\nu_{\mu}$ , $\bar{\nu}_{\mu}$	$\# \nu_e, \bar{\nu}_e \text{ files}$	# of $\nu_{\mu}, \bar{\nu}_{\mu}$ files
6CM	$6\mathrm{cm}$	$6\mathrm{cm}$	10	30
$12\mathrm{CM}$	nue	numu	10	30
DOUBLE	double	$\operatorname{double}$	10	50
XORY	xory	xory	10	30
12BAR	$\operatorname{nuebar}$	numubar	10	9

## 3 The beam spectra and oscillation parameters used

In the subsequent analysis the detector was assumed to be located  $10 \,\mathrm{km}$  off-axis at  $732 \,\mathrm{km}$ . The beam spectra used to weight the events are in arrays of  $1000 \,\mathrm{bins}$  of  $20 \,\mathrm{MeV}$  between 0 and  $20 \,\mathrm{GeV}$  stored in files to be found in the directory:

/afs/fnal.gov/files/code/off-axis/off-axis\_01/beam The files used are;

•  $\nu_{\mu}$  spectrum: **me\_numu\_r10e5\_z735e5.vec** 

This file was used for three different purposes:

- It was used to weight the generated  $\nu_{\mu}$ CC events in order to study the background from these events. However, since the  $\nu_{\mu}$  spectrum at long baselines is depleted though oscillations to  $\nu_{\tau}$ , for this source of background, the weight read from the file was multiplied by the survival probability for a  $\nu_{\mu}$  at that distance and energy:

$$1.0 - \sin^2 2\theta_{\mu\tau} \sin^2 \frac{1.27\Delta m^2 L}{E_{\nu}}$$

with

$$\sin^2 2\theta_{\mu\tau} = 1.0$$
 and  $\Delta m^2 = 2.5 \times 10^{-3} \text{ eV}^2$ .

- It was also used to weight the generated  $\nu_{\mu}NC$  events to study the background from this source. No survival probability was needed here since  $\nu_{\mu}NC$  and  $\nu_{\tau}NC$  events are identical.
- Finally it was used to weight the generated  $\nu_e CC$  events in order to study the  $\nu_{\mu} \rightarrow \nu_e$  signal events. Here the weight read from the file was multiplied by the  $\nu_{\mu} \rightarrow \nu_e$  oscillation probability. This was taken to be:

$$\sin^2\theta_{23}\sin^22\theta_{13}\sin^2\frac{1.27\Delta m^2L}{E_{\nu}}$$

which becomes for  $\theta_{23} = 45$  degrees, and  $sin^2 2\theta_{13} = 0.1$  (the CHOOZ' limit):

$$0.05\sin^2\frac{1.27\Delta m^2L}{E_{\nu}}$$

•  $\nu_e$  spectrum: me\_nue\_r10e5\_z735e5.vec

This was used to weight the generated  $\nu_e$ CC events in order to study the background from the intrinsic  $\nu_e$  in the beam.

When running at a yearly rate of  $4.0 \times 10^{20}$  protons on target the  $\nu_{\mu}$  file gave 107.594  $\nu_{\mu}$ CC events per kiloton. year and the  $\nu_{e}$  file gave a rate of 2.177  $\nu_{e}$ CC events per kiloton. year.

Similarly for the antineutrino run the files used were:

- $\bar{\nu}_{\mu}$  spectrum: me\_anti\_numubar\_r10e5\_z735e5.vec
- $\bar{\nu}_e$  spectrum: me\_anti\_nuebar\_r10e5\_z735e5.vec

with the corresponding normalizations of **32.378**  $\bar{\nu}_{\mu}$ CC events and **0.707**  $\bar{\nu}_{e}$ CC events per kiloton.year.

It should be noted that the background from the minor components of the beam (anti-neutrinos in neutrino running) was not included in these calculations except in the section dealing with the comparison of neutrino and antineutrino running. The contribution of  $\nu_{\mu}$  and  $\nu_{e}$  is indeed important in antineutrino running and cannot be neglected.

## 4 The overall background rejection strategy

The strategy was to reduce the  $\nu_{\mu}$ NC background to a level below that of the intrinsic  $\nu_e$  in the beam, while keeping the signal  $\nu_e$ CC efficiency as high as possible. This was done in two steps: loose cuts followed by the use of likelihood functions to distinguish between signal  $\nu_e$ CC and background  $\nu_{\mu}$ NC events. The purpose of the loose cuts was twofold. Some of them were used to reject  $\nu_{\mu}$ CC and beam  $\nu_e$ CC events. In addition they all served in defining a definite range of variables for the likelihood functions used in the second step.

For each of the configurations, half of the files available were used to study the background, define the loose cuts, generate the probability density functions used in the likelihood functions and decide on the cut on this likelihood that maximized the sensitivity of the experiment. The cuts and likelihood functions were then applied to the second half of the files, thus obtaining an unbiased measure of the sensitivity. The following variables were defined based on the variables available in the ntuples and described in [1]:

 $\mathbf{ang} = \sqrt{(\mathrm{angx}^2 + \mathrm{angy}^2)}$ , the three-dimensional angle of the candidate electron with respect to the beam.

**tothit** = nhit\_x + nhit\_y, total number of hit strips in the event.

**ensumht** = h\_roa\_x + h\_roa\_y, total number of hit strips associated to the electron candidate (the track with the largest number of hit strips).

 $\mathbf{why} = \text{ensumht/tothit}$ , the fraction of the event hits associated to the electron candidate.

**chimax**, the maximum of chix and chiy, the  $\chi^2$  of the fits to the electron candidate track in the x and y views.

 $\mathbf{peet} = \sqrt{(\text{peet\_x}^2 + \text{peet\_y}^2)}$ , the overall net transverse momentum of the event.

**emult** = ensumht/(nplx+nply), the mean number of hit strips per plane associated to the candidate electron.

**plgapmin**, the lowest of plgapx and plgapy, provided they were not zero. plgapx and plgapy are the last hit gap before the first gap encountered along the track.

#### 5 The loose cuts

Clearly the value of some of the above variables depended on the sampling frequency. Therefore some of the cuts used were configuration dependent.

### 5.1 Configuration-independent cuts

The following cuts were the same for all configurations:

1.3 < emult < 3.0 The lower cut is tighter than necessary for NC rejection but is necessary for rejecting muons in  $\nu_{\mu}$ CC events. This can be seen in Fig. 2.

ang < 2.0 chimax < 100.0  $plgapmin \neq 1.0$ 

#### 5.2 Configuration-dependent cuts

The next set was configuration dependent:

#### $\mathbf{ensumht}$

The range of ensumht for accepted events is given in the second column of Table 3. For events with  $\mathbf{why} > \mathbf{0.95}$  a tighter cut was applied: ensumht had to be larger than the value given in the third column of the table.

#### tothit

This is equivalent to a total energy cut.

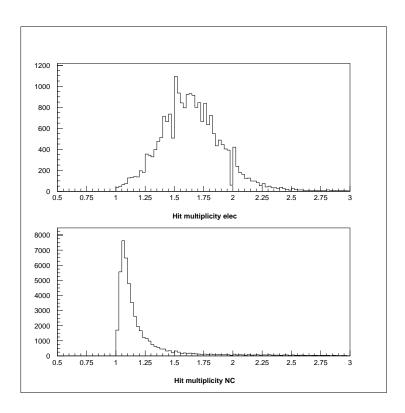


Figure 2: The mean number of hit strips per plane associated to the track. Top plot for signal electrons and bottom plot for CC background

The upper cut on this variable is tighter than necessary for NC rejection but is necessary for rejecting intrinsic  $\nu_e$ CC events which are mostly of higher energy than the signal  $\nu_e$ CC. This can be seen in Fig. 3. **peet** 

### 6 The likelihood functions

Having applied these cuts, three two-dimensional probability density functions (pdf) were generated for signal events (PS) and for  $\nu_{\mu}$ NC events (PB). The pdf's used were:

- ensumht vs why referred to as PS(sy) and PB(sy), Fig. 4.
- ang vs tothit referred to as PS(at) and PB(at), Fig. 5.
- chimax vs plgapmin referred to as PS(cp) and PB(cp), Fig. 6.

Table 3: Cut values for ensumht

Configuration	Cut range	why $>0.95$ events		
$6\mathrm{CM}$	35 < ensumht < 180	60		
$12\mathrm{CM}$	24 < ensumht < 100	40		
DOUBLE	12 < ensumht < 50	20		
XORY	12 < ensumht < 50	20		

Table 4: Cut values for tothit

Configuration	Cut range
6CM	60 < tothit < 200
$12\mathrm{CM}$	32 < tothit < 100
DOUBLE	16 < tothit < 50
XORY	16 < tothit < 50

The procedure to generate each pdf was to generate a two-dimensional histogram of the relevant variables, smooth it and normalize it to unity.

Given the values of the 6 variables, ensumbt, why, ang, to thit, chimax and plgapmin, of an event, the probability that the event was of signal origin was computed as:

$$PS(sy) \times PS(at) \times PS(cp)$$

Similarly the probability of the event being of background origin was:

$$PB(sy) \times PB(at) \times PB(cp)$$

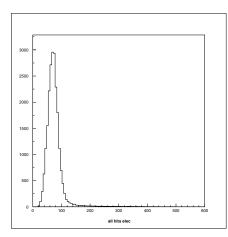
and the likelihood was:

$$L = \log(\frac{PS(sy) \times PS(at) \times PS(cp)}{PB(sy) \times PB(at) \times PB(cp)})$$

Note that different pdf's were calculated and used for each of the five configurations. The kumacs to generate the likelihoods for the signal  $\nu_e$  CC and the

Table 5: Cut values for peet

Configuration	Cut range
6CM	peet < 80
$12\mathrm{CM}$	peet < 40
DOUBLE	peet < 20
XORY	peet < 20



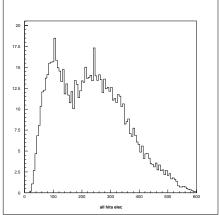


Figure 3: The distribution of total hits in the event for signal  $\nu_e$  (left plot) and intrinsic beam  $\nu_e$  (right plot)

fortran routines they call are named:

likelsyxxxx.kumac, likelatxxxxx.kumac and likelcpxxxxx.kumac.

likelsyxxxx.for, likelatxxxxx.for and likelcpxxxxx.for.

where xxxxx stands for 6cm, 12cm, double, 12xory and 12bar.

They produce pdf arrays called:

likelsy.xxxxx, likelat.xxxxx and likelcp.xxxxx.

The corresponding names for the NC background are:

likncsyxxxx.kumac, likncatxxxxx.kumac and likncepxxxxx.kumac.

likncsyxxxx.for, likncatxxxxx.for and liknccpxxxxx.for.

likncsy.xxxxx, likncat.xxxxx and likncep.xxxxx.

The pdf functions were then used on the unbiased sample of events by running the following kumac and fortran routines:

chainxxxxx.kumac and chainxxxxx.for for signal  $\nu_e$  CC and NC background, and

chainnuexxxxx.kumac and chainnuexxxxx.for for intrinsic beam  $\nu_e$  CC.

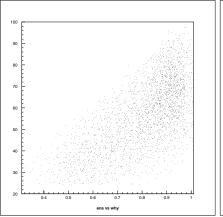
All these routines and likelihood functions as well as links to the event files directories can be found in the directory:

/afs/fnal/files/code/off-axis/off-axis\_01/code/analysis

An example of the signal and NC background likelihoods for the 12CM configuration is shown in Fig 7. In this case a cut on the likelihood of 3.25 was chosen (see next section).

#### 7 Results

A Figure of Merit (FOM) was defined as:



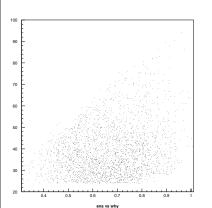


Figure 4: The ensumbt vs why pdf two-dimensional distribution for signal(left plot) and NC background (right plot)

$$FOM = \frac{Number of signal events}{\sqrt{Total number of background events}}$$

The FOM was calculated assuming:

- $4.0 \times 10^{20}$  protons on target per year
- a 5 year run
- a 50 kiloton detector
- an 85% fiducial mass.

For each configuration, the numbers of signal events and of background  $(\nu_{\mu} NC, \nu_{\mu} CC)$  and beam  $\nu_{e}$ , and, from these, the FOM were calculated as a function of likelihood cut. The FOM is a slowly varying function of the likelihood cut as is shown in the example of Fig. 8. However the background changes by a factor of three over this range of likelihood cut and the signal by a factor of two as can be seen in Fig. 8. The cut that gave the maximum FOM was selected and used in the analysis of the unbiased event files

The signal efficiency and background rejection obtained are listed in Table 6 for the 12CM configuration as an example.

With the detector and running scenario listed above the expected number of produced events are as follows:

Events = Flux x Years x Mass x Fiducial

Number of  $\nu_{\mu}$ CC events before oscillations:

 $107.594 \times 5 \times 50 \times 0.85 = 22863.7$ 

Number of intrinsic beam  $\nu_e$ CC events:

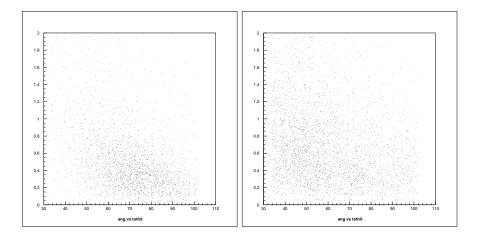


Figure 5: The ang vs to thit pdf two-dimensional distribution for signal (left plot) and NC background (right plot)

Table 6: Signal efficiency and background rejection for the 12CM configuration

	Bacl	Background Rejection					
Signal efficiency	$ u_{\mu}$ NC	$ u_{\mu} \mathrm{CC}$	Beam $\nu_e$				
0.35	$1.9 \times 10^{-3}$	$5.6 \times 10^{-4}$	$5.6 \times 10^{-2}$				

 $2.177 \times 5 \times 50 \times 0.85 = 462.6$ 

Number of  $\nu_{\mu} \rightarrow \nu_{e}$  signal events:

Events =  $\nu_{\mu}$ CC events x oscillation prob.

 $22863.7 \times 0.0293 = 669.7$ 

The numbers of signal events and of background events from the three sources at the optimum FOM are shown in Table 7 for the four configurations, assuming the running conditions listed above.

## 8 The sensitivity as a function of absorber thickness

Three configurations were used in this analysis; 6CM,12CM and DOUBLE.

The results are shown in Table 8.

The uncertainty on these numbers is less than 1.0. Whereas reducing the absorber thickness by a factor of two does not improve the sensitivity significantly, doubling the thickness does worsen it by 21%.

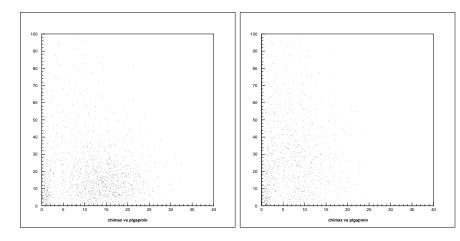


Figure 6: The chimax vs plgapmin pdf two-dimensional distribution for signal(left plot) and NC background (right plot)

Table 7: Numbers of signal and background events at the optimum FOM

			$\operatorname{Background}$				
Configuration	$_{ m Signal}$	$\nu_{\mu}$ NC	$\nu_{\mu} CC$	Beam $\nu_e$	Sum backg.	FOM	
6CM	208.9	7.6	2.1	24.3	34.0	35.8	
$12\mathrm{CM}$	232.2	12.9	5.3	25.8	44.0	35.0	
DOUBLE	217.7	20.6	8.7	27.3	56.6	28.9	
XORY	213.6	13.6	4.9	24.3	42.8	32.6	

# 9 The sensitivity as a function of active plane positions

Given a certain number of active readout planes, is it better to have both an x and a y plane together every D(cm) of aborber, Fig 9, or to alternate x and y every 0.5D(cm) of absorber, Fig 10?

Separating the x and y planes rather than lumping them together improves the FOM by 10%.

The origin of this improvement was investigated. The effect of the loose cuts was the same on the two configurations. It was only after the likelihoods that the improvement was seen. This was due equally to the **ensumht vs why** and the **ang vs tothit** likelihoods. The reason for this improvement was traced to an improvement in the energy resolution of the detector when using a finer sampling, even though at each sampling only an x or a y are available. It goes from 17.2% in the DOUBLE configuration that samples every 0.6 rad. length to 15.0% in the XORY configuration that samples every 0.3 rad. length.

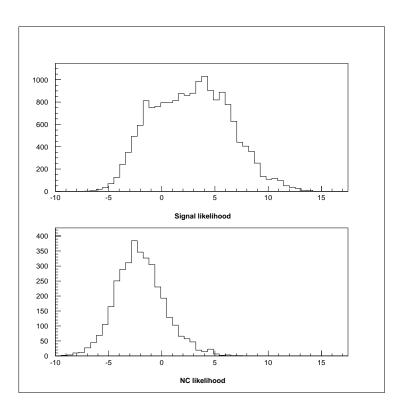


Figure 7: The signal and NC likelihoods for the 12CM configuration

## 10 Differences between $u_{\mu} \rightarrow u_{e}$ and $\bar{\nu}_{\mu} \rightarrow \bar{\nu}_{e}$

Since determining  $\theta_{13}$  and  $\delta_{CP}$  will require antineutrino running as well as neutrinos, the performance of the detector for antineutrinos was also investigated. Antineutrino events were generated, ntuples were produced and likelihoods were computed in the same way as described for neutrinos using the 30% radiation length geometry. This sample is referred to as 12BAR and is to be compared to the neutrino 12CM configuration.

As explained earlier the background arising from the  $\nu_{\mu}$  and  $\nu_{e}$  components of the antineutrino beam had to be taken into account. For completeness the background from the  $\bar{\nu}_{\mu}$  and  $\bar{\nu}_{e}$  components of the neutrino beam were also computed.

The corresponding normalization beam flux files were:

- $\nu_{\mu}$  in antineutrino running: me\_anti\_numu\_r10e5\_z735e5.vec
- $\nu_e$  in antineutrino running: me\_anti\_nue\_r10e5\_z735e5.vec

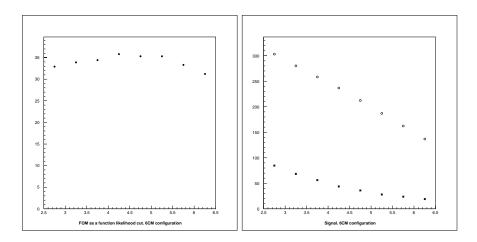


Figure 8: Left plot: The Figure of Merit as a function of likelihood cut. Right plot: The numbers of signal (open circles) and background (asterisk) events as a function of likelihood cut

Table 8: Dependence of the Figure of Merit on the Sampling Frequency

Configuration	Radiation length $(\%)$	Likelihood Cut	FOM
6CM	17.5	4.50	35.8
$12\mathrm{CM}$	30	3.25	35.0
DOUBLE	60	2.50	28.9

- $\bar{\nu}_{\mu}$  in neutrino running: me\_numubar\_r10e5\_z735e5.vec
- $\bar{\nu}_e$  in neutrino running: me\_nuebar\_r10e5\_z735e5.vec

The signal efficiency and background rejection at the best FOM are summarized in Table 10.

The signal efficiency for a comparable level of major component background rejection is much better in antineutrino running. This is because of the hadronic

Table 9: Dependence of the Figure of Merit on the active plane position

Configuration	Likelihood Cut	FOM
DOUBLE	2.50	28.9
XORY	3.00	32.6

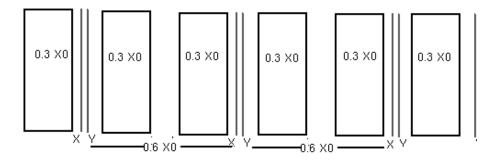


Figure 9: x and y plane together

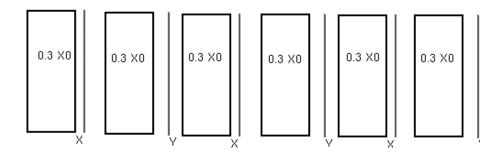


Figure 10: x or y plane alternating

energy in antineutrino events being lower, on average, than in neutrino events. The probability to simulate a signal electron of appreciable energy is therefore reduced in antineutrino events. However the background from the minor component ( $\nu_{\mu}$  and beam  $\nu_{e}$ ) is of comparable magnitude to the major component background.

The expected numbers of produced events for a 5 year antineutrino run are: **6880.3**  $\bar{\nu}_{\mu}$ CC events, **150.24** intrinsic beam  $\bar{\nu}_{e}$ CC events and **192.2** signal  $\bar{\nu}_{e}$ CC events.

Folding efficiencies and rejections results in the numbers of expected events shown in Table 11.

Thus, to have comparable significance in neutrino and antineutrino running, the antineutrino run will have to be  $(33.8/19.7)^2$  times as long as the neutrino run, i.e.  $\sim 3.0$  times longer.

Table 10: Comparison of the neutrino and antineutrino signal efficiencies and background rejections for the  $12\mathrm{CM}$  configuration

Table 11: A comparison of the numbers of events expected in neutrino and antineutrino running

			$\operatorname{Background}$						
		Majo	Major component Minor component						-
		$ u_{\mu}$	$ u_{\mu}   u_{\mu}   u_{e}   u_{\mu}   u_{\mu}   u_{e}   $ Sum						
Conf.	$_{ m Signal}$	NC	CC	$\operatorname{Beam}$	NC	CC	$\operatorname{Beam}$	backg.	FOM
12CM	232.2	12.9	5.3	25.8	1.6	0.0	1.5	47.1	33.8
12BAR	96.1	4.6	4.6 0.8 10.1 4.3 0.6 3.3 23.7						

## References

[1] L. Camilleri, A. Para. The Reconstruction of  $\nu_{\mu}$  and  $\nu_{e}$  Monte Carlo events. Off-Axis-NOTE-SIM-11.